# STUDY OF OVERTAKING ON SLIPPERY TWO-LANE ROAD 

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## 1. Abstract

In winter, slippery roads emerge in cold regions like Hokkaido. The braking distance on these roads exceeds that on dry roads. Accordingly, the Road Structure Act provides that the braking distance on slippery roads be calculated in consideration of the decline in the friction coefficient between tire and road surface.

It also becomes more difficult for vehicles to accelerate and decelerate on slippery roads. Accordingly, calculation of PSD on slippery roads should consider the decline in friction coefficient. However, the Road Structure Act does not provide for such consideration. Furthermore, aborting of overtaking caused by the perception error of driver should be analyzed comprehensively on roads of two opposing lanes.

In this study, a model of overtaking model and a model of aborting overtaking that consider the slippery road are developed. The following conclusions were obtained. The length of overtaken vehicle, the speed of overtaking vehicle and the friction coefficient between tire and road surface have a large effect on the PSD, but the ascent slope does has no such effect. The speed of overtaking vehicle and the friction coefficient between tire and road surface have a large effect on the aborting safety ratio, which indicates the difficulty of aborting, but the ascent slope and the length of vehicle have no such effect.

## 2. Introduction

In winter, slippery roads emerge in cold regions like Hokkaido. The braking distance on these roads is greater than on dry roads. Accordingly, the Road Structure Act provides that, on slippery road, this distance be calculated in consideration of the decline in friction coefficient between tire and road surface.

On slippery roads it becomes more difficult for vehicles to accelerate and decelerate. Accordingly, calculation of PSD on such roads should consider the decline in friction coefficient. However, the Road Structure Act does not provide for such consideration. Furthermore, aborting of overtaking caused by the perception error of driver should be analyzed comprehensively on a road of two opposing lanes.

This study developed an overtaking model for slippery roads. The vehicle acceleration is calculated using both the friction coefficient between tire and road surface and the driving performance curve. The vehicle length, the reaction time of driver and the ascent slope are incorporated into the model. Under the supposition that there is perception error of driver regarding the speed of oncoming vehicle and the PSD, a model of aborting overtaking also is developed, which defines the safe distance to abort. The ratio of the safe distance to abort to the PSD is defined as the aborting safety ratio. The model analyzes aborting.

## 3. Overtaking model (2)

- Maximum acceleration of vehicle

When the driving force of vehicle $T$ exceeds the driving resistance $R$, i.e. when $T-R>0$, the vehicle accelerates. In this case, the maximal acceleration $a_{M A X}\left[\mathrm{~m} / \mathrm{s}^{2}\right]$ is calculated by Eq. 1 .

$$
\begin{equation*}
a_{M A X}=g \cos \theta(T-R) /(W+\Delta W) \quad\left[\mathrm{m} / \mathrm{s}^{2}\right] \tag{1}
\end{equation*}
$$

where $W, \Delta W, g$ and $\theta$ indicate the weight of vehicle, the weight of vehicle's wheel assembly (tire, wheel, axle), the acceleration due to gravity and the ascent slope ( $i \%$ ), respectively. The maximum acceleration $a_{S U P}\left[\mathrm{~m} / \mathrm{s}^{2}\right]$ is calculated by Eq. 2, because slipping arises in the case of $T$ $-R>\mu_{t} W_{R}$.

$$
\begin{equation*}
a_{S U P}=g \cos \theta \mu_{t} W_{R} /(W+\Delta W) \quad\left[\mathrm{m} / \mathrm{s}^{2}\right] \tag{2}
\end{equation*}
$$

where $\mu_{t}$ and $W_{R}$ indicate the friction coefficient between tire and road surface and the partial weight of drive wheel. When the ascent slope is gentle, it can be supposed that $g \cos \theta \fallingdotseq g, a_{M A X}$ and $a_{S U P}$ are approximated by Eq. 3 and Eq. 4, respectively.

$$
\begin{align*}
& a_{M A X}=g(T-R) /(W+\Delta W) \quad\left[\mathrm{m} / \mathrm{s}^{2}\right]  \tag{3}\\
& a_{S U P}=g \mu_{t} W_{R} /(W+\Delta W) \quad\left[\mathrm{m} / \mathrm{s}^{2}\right] \tag{4}
\end{align*}
$$

It is supposed that $\Delta W / W=0.08$, after the fashion of Japanese Industrial Standards (JIS). Accordingly, the maximal acceleration considering the friction coefficient between tire and road surface $a_{\max }\left[\mathrm{m} / \mathrm{s}^{2}\right]$ is calculated by Eq. 5 .

$$
\begin{equation*}
a_{\max }=\min \left(a_{M A X}, a_{S U P}\right) \quad\left[\mathrm{m} / \mathrm{s}^{2}\right] \tag{5}
\end{equation*}
$$

The driving force of vehicle $T$ is calculated by Eq. 6 (1).

$$
\begin{equation*}
T=\frac{270}{V_{m}} H \eta\left\{1.1-1.1\left(\frac{V}{V_{m}}-0.7\right)^{2}\right\} \quad[\mathrm{kg}] \tag{6}
\end{equation*}
$$

where $H$ [PS], $V[\mathrm{~km} / \mathrm{h}]$ and $V_{m}[\mathrm{~km} / \mathrm{h}]$ indicate the maximum power output of vehicle, the speed of vehicle and the speed of vehicle at maximum engine rev. These numbers are obtained from the driving performance curve of vehicle.

It is supposed that the driving resistance $R$ consists of the air resistance, the rolling resistance and the resistance due to gravity. Eq. 7 expresses the driving resistance $R$.

$$
\begin{equation*}
R=W \sin \theta+W \cos \theta \mu_{r}+\lambda S V^{2} \quad[\mathrm{~kg}] \tag{7}
\end{equation*}
$$

Where $\mu_{r}, S$ and $\lambda$ indicate the rolling resistance coefficient, forward surface area of vehicle and the air resistance coefficient, respectively. When the ascent slope is gentle it can be supposed that $\sin \theta \fallingdotseq i / 100$ and $\cos \theta=1.0$. $R$ is approximated by Eq. 8 .

$$
\begin{equation*}
R=(W / 100) i+W \mu_{r}+\lambda S V^{2} \tag{8}
\end{equation*}
$$

## - Development of overtaking model

The following five assumptions are made for the purpose of calculating PSD.
(1) At the start of overtaking, the overtaking vehicle is driving on a road of two opposing lanes at the same speed as the overtaken vehicle.
(2) The overtaking vehicle accelerates to the overtaking speed when it starts overtaking.
(3) The lengths of the overtaking vehicle and the overtaken vehicle should be introduced.
(4) The reaction time of driver should be introduced.
(5) The safety distance between vehicles should be introduced.
$P S D$ comprises the following four distances and is expressed (in meters) by Eq. 9 (Fig. 1).

$$
P S D=d_{1}+d_{2}+d_{3}+d_{4}
$$

Figure 1. PSD


These distances are calculated based on the space headway of vehicles, because of the introduction of vehicle lengths.
$d_{l}$ : The driving distance between the point where the overtaking driver judges that overtaking is possible and enters the opposing lane to accelerate, and the point where the speed of the overtaking vehicle reaches the overtaking speed.

The $d_{l}$ is calculated by Eq. 10 .

$$
\begin{equation*}
d_{l}=(1 / 3.6) V_{0}\left(t_{1}+\varepsilon_{1}\right)+(1 / 2) a t_{1}^{2} \tag{10}
\end{equation*}
$$

where $V_{0}[\mathrm{~km} / \mathrm{h}], a\left[\mathrm{~m} / \mathrm{s}^{2}\right], \varepsilon_{l}[\mathrm{sec}]$ and $t_{1}[\mathrm{sec}]$ indicate the speed of overtaken vehicle, the average acceleration of overtaking vehicle, the reaction time of overtaking driver and the acceleration duration, respectively.
$d_{2}$ : The driving distance between the point where the overtaking vehicle reaches overtaking speed and the point where the overtaking vehicle reenters the cruising lane at a safe distance from the overtaken vehicle. The $d_{2}$ is calculated by Eq. 10 .

$$
\begin{equation*}
d_{2}=(1 / 3.6) V t_{2} \tag{11}
\end{equation*}
$$

where $V[\mathrm{~km} / \mathrm{h}]$ and $t_{2}[\mathrm{sec}]$ indicate the overtaking speed and the duration of overtaking speed, respectively.
$d_{3}$ : The safe distance between the overtaking vehicle and the oncoming vehicle when the overtaking is completed. These distances are determined after the fashion of the Road Structure Act (Table 1) (1).

Table 1. Safe distance

| speed of overtaking vehicle $(\mathrm{km} / \mathrm{h})$ | 80 | 60 | 40 |
| :--- | :--- | :--- | :--- |
| speed of overtaken vehicle $(\mathrm{km} / \mathrm{h})$ | 65 | 45 | 30 |
| safe distance $(\mathrm{m})$ | 60 | 40 | 25 |

$d_{4}$ : The distance driven by the oncoming vehicle until the overtaking vehicle completes the overtaking. The $d_{4}$ is calculated by Eq. 12 .

$$
\begin{equation*}
d_{4}=(1 / 3.6) V\left(t_{1}+t_{2}+\varepsilon_{1}\right) \tag{12}
\end{equation*}
$$

In Fig. $1, L_{1}$ and $L_{2}$ indicate the safe distance for stopping in our model. It is supposed that Eq. 13 expresses $L_{1}$ and $L_{2}$.

$$
\begin{align*}
S_{m} & =l+\frac{v}{3.6}+\frac{v^{2}}{2 g \mu_{t} * 3.6^{2}} \\
L_{1} & =L_{2}=S_{m} \quad \text { on dry surface } \\
L_{1}=L_{2} & =\min \left(S_{m}, 70\right) \quad \text { on slippery surface } \tag{13}
\end{align*}
$$

where $S_{m}[\mathrm{~m}], l[\mathrm{~m}]$ and $v[\mathrm{~km} / \mathrm{h}]$ indicate the safe space headway, the distance where the following vehicle can stop safely if the leading vehicle stops suddenly (provided by the Road Structure Act), and the speed of following vehicle, respectively (1). When $L_{1}$ and $L_{2}$ are considered in the model, $t_{2}$ and $d_{2}$ are calculated by Eq. 14 and Eq. 15, respectively.

$$
\begin{align*}
& t_{2}=3.6\left(d_{a}+L_{1}+L_{2}-d_{1}\right) /\left(V-V_{0}\right)  \tag{14}\\
& d_{2}=(1 / 3.6) V t_{2} \tag{15}
\end{align*}
$$



Figure 2. Real space headway considering the length of vehicles
where $d_{a}$ indicates the distance that the overtaken vehicle drives during $t_{1}+t_{2}+\varepsilon_{1}$ and is expressed by Eq. 16 .

$$
d_{a}=(1 / 3.6) V_{0}\left(t_{1}+t_{2}+\varepsilon_{1}\right) \quad 16
$$

Let $l_{1}[\mathrm{~m}]$ and $l_{2}[\mathrm{~m}]$ be the lengths of the overtaking vehicle and the overtaken vehicle, respectively. In this case, real space headway $L_{1}{ }^{*}$ and $L_{2}{ }^{*}$ are calculated by Eq. 17 and Eq. 18, respectively (Fig.2).

$$
\begin{align*}
& L_{1} *=L_{1}+l_{2}  \tag{17}\\
& L_{2}{ }^{*}=L_{2}+l_{1} \tag{18}
\end{align*}
$$

## 4. Model for aborting of overtaking (2)

## - The maximal deceleration of vehicle

It is supposed that the maximal deceleration of vehicle $d_{\max }\left[\mathrm{m} / \mathrm{s}^{2}\right]$ is determined by the weight of vehicle, the friction coefficient between tire and road surface and the ascent slope. The $d_{\text {max }}$ is calculated by Eq. 19 in this model.

$$
\begin{align*}
d_{\max } & =\left(g \mu_{t} W \cos \theta+W \sin \theta\right) /(W+\Delta W) \\
& \fallingdotseq\left(g \mu_{t} W+W i / 100\right) /(W+\Delta W) \quad\left[\mathrm{m} / \mathrm{s}^{2}\right] \tag{19}
\end{align*}
$$

## - Model of avoidance of overtaking

The following five assumptions are made.
(1) There is the perception error by overtaking driver: The PSD perceived by the overtaking driver is shorter than the real $P S D$, and the speed of the oncoming vehicle perceived by the overtaking driver is less than the real speed.
(2) The lengths of overtaking vehicle and overtaken vehicle should be introduced.
(3) The reaction time of driver should be introduced.
(4) The safety distance between vehicles should be introduced
(5) The minimum speed of the overtaking vehicle should be introduced.

Consider the case of the overtaking driver beginning to abort $t_{a}$ [sec] after starting overtaking. It is supposed that the reaction time of the overtaking driver is $\varepsilon_{2}[\mathrm{sec}]$ and the space headway between the overtaking vehicle and the overtaken vehicle after $\left(t_{a}+\varepsilon_{2}\right)$ [sec] is $x_{a}[\mathrm{~m}]$. The $x_{a}$ has positive value when the overtaken vehicle is in front of the overtaking vehicle. The $x_{a}$ and the speed of the overtaking vehicle at the time $V_{a}$ should be considered in two cases: that where the overtaking vehicle is accelerating (Fig. 3), and that where it is not accelerating (Fig. 4). Eq. 20 and Eq. 21 express $x_{a}$ and $V_{a}$ in each case, where $V_{\text {min }}$ in Fig. 3 and Fig. 4 indicates the
minimal speed of the overtaking vehicle and is supposed as $20[\mathrm{~km} / \mathrm{h}]$.

$$
\begin{gather*}
\text { when } \varepsilon_{1}<t_{a}+\varepsilon_{2} \leqq \varepsilon_{1}+t_{1}, x_{a}=L_{1}+l_{2}-0.5 a\left(t_{a}-\varepsilon_{1}+\varepsilon_{2}\right)^{2} \\
V_{a}=V_{0}+3.6 a\left(t_{a}-\varepsilon_{1}+\varepsilon_{2}\right)  \tag{20}\\
\text { when } t_{a}+\varepsilon_{2}>\varepsilon_{1}+t_{1}, x_{a}=L_{1}+l_{2}-\left[0.5 a t_{1}{ }^{2}+\left\{\left(V-V_{0}\right) / 3.6\right\}\left(t_{a}-\varepsilon_{1}+\varepsilon_{2}-t_{1}\right)\right] \\
V_{a}=V \tag{21}
\end{gather*}
$$

The time $t_{c}$ [sec] indicates the time interval between when the overtaking driver starts overtaking and when the space headway between the oncoming vehicle and the overtaking vehicle equals 0 . Eq. 22 expresses $t_{c}$ on the supposition that perception error regarding $P S D$ and the speed of oncoming vehicle are $\Delta d[\mathrm{~m}]$ and $\Delta v[\mathrm{~km} / \mathrm{h}]$, respectively (Fig. 5).

$$
\begin{equation*}
t_{c}=\left(P S D-\Delta d-L_{1}-l_{2}\right) /\left\{\left(V_{0}+V+\Delta v\right) / 3.6\right\} \tag{20}
\end{equation*}
$$

It is supposed that aborting should be finished by the time the space headway between the oncoming vehicle and the overtaken vehicle equals 0 . That is, the time interval of $t_{c}-\left(t_{a}+\varepsilon_{2}\right)$ is allowed for the overtaking driver to finish aborting. The time interval of adt [sec] that is required for the overtaking vehicle to decelerate to the minimal speed is calculated by Eq. 23.

$$
\begin{equation*}
a d t=\left(V_{a}-V_{\text {min }}\right) /\left(3.6 a_{d}\right) \tag{23}
\end{equation*}
$$

where $a_{d}$ indicates the deceleration of the overtaking vehicle. The $d_{f}$ and $d_{s}$ indicate the driving


Figure 3. Time-speed relationship of aborting when the overtaking vehicle accelerates


Figure 5. Relationship between the oncoming and the overtaking vehicle


Figure 4. Time-speed relationship of aborting when the overtaking vehicle drives at the overtaking speed


Figure 6. The relative distance when aborting finishes
distance of the overtaking vehicle and that of the overtaken vehicle during time interval $t_{c}-\left(t_{a}+\right.$ $\varepsilon_{2}$ ), respectively. These distances should be considered in two cases: that where the overtaking vehicle needs to decelerate to the minimum speed, and that where the overtaking vehicle need not decelerate to the minimum speed. These are calculated by Eq. 24 and Eq. 25, respectively.

In both cases, the condition for safely finishing the aborting considering the vehicle lengths is expressed by Eq. 26 (Fig. 6).

$$
\begin{equation*}
x_{a}+\left(d_{s}-d_{f}\right)-\left(L_{3}+l_{2}\right) \geqq 0 \tag{26}
\end{equation*}
$$

where $L_{3}$ indicates the safe distance expressed by Eq. 27 .

$$
\begin{equation*}
L_{3}=\min \left(L_{1}, 70\right) \tag{27}
\end{equation*}
$$

The $t_{a}^{\text {max }}$ indicates the maximal time that satisfies Eq. 24. We define the safe distance to abort as $D_{a}[\mathrm{~m}]$ and the aborting safety ratio as $D_{R}$ [\%]. $D_{a}$ indicates the driving distance of the overtaking vehicle during time interval $t_{a}{ }^{\max }+\varepsilon_{2}$. Eq. 28 and Eq. 29 yield $D_{R}$ and $D_{a}$, respectively.

$$
\begin{equation*}
D_{R}=D_{a} / P S D \tag{28}
\end{equation*}
$$

$$
\text { when } t_{a}{ }^{\max }+\varepsilon_{2} \leqq t_{1}+\varepsilon_{1}, D_{a}=\left(V_{0} / 3.6\right)\left(t_{a}{ }^{\max }+\varepsilon_{2}\right)+0.5 a\left(t_{a}{ }^{\max }-\varepsilon_{1}+\varepsilon_{2}\right)^{2}
$$

$$
\text { when } t_{a}^{\max }+\varepsilon_{2}>t_{1}+\varepsilon_{1}, D_{a}=\left(V_{0} / 3.6\right)\left(t_{1}+\varepsilon_{1}\right)+0.5 a\left(t_{1}-\varepsilon_{1}\right)^{2}
$$

$$
\begin{equation*}
+(V / 3.6)\left(t_{a}^{m a x}+\varepsilon_{2}-t_{1}-\varepsilon_{1}\right) \tag{29}
\end{equation*}
$$

$D_{R}$ indicates that the smaller $D_{R}$ becomes, the more difficult it becomes to abort.

## 5. Computer simulation

## - Settings

Computer simulations were conducted under the three conditions of road surface: dry, snowy and icy. Their friction coefficients are shown in Table 2 (2). Table 3 shows the values used to calculate the driving resistance of overtaking vehicle.

Table 2. Friction coefficient between tire and road surface

| condition of surface | dry | snowy | icy |
| :---: | :---: | :---: | :---: |
| friction coefficient | 0.7 | 0.3 | 0.2 |

$$
\begin{align*}
& \text { when } t_{c}-\left(t_{a}+\varepsilon_{2}\right)>a d t d_{f}=\left\{\left(V_{a}-3.6 a_{d} \cdot a d t\right) / 3.6\right\}\left(t_{c}-t_{a}-\varepsilon_{2}\right)+0.5 a_{d} \cdot a d t^{2} \\
& d_{s}=\left(V_{0} / 3.6\right)\left(t_{c}-t_{a}-\varepsilon_{2}\right)  \tag{24}\\
& \text { when } \quad t_{c}-\left(t_{a}+\varepsilon_{2}\right) \leqq a d t d_{f}=\left\{\left(V_{a}-3.6 a_{d}\left(t_{c}-t_{a}-\varepsilon_{2}\right)\right) / 3.6\right\}\left(t_{c}-t_{a}-\varepsilon_{2}\right)+0.5 a_{d}\left(t_{c}-t_{a}-\varepsilon_{2}\right)^{2} \\
& d_{s}=\left(V_{0} / 3.6\right)\left(t_{c}-t_{a}-\varepsilon_{2}\right) \quad 25
\end{align*}
$$

Table 3. Values used to calculate driving resistance

| weight of <br> vehicle $(\mathrm{t})$ | coefficient of <br> rolling resistance | coefficient of air <br> resistance | forward surface area <br> of vehicle $\left(\mathrm{m}^{2}\right)$ |
| :---: | :---: | :---: | :---: |
| 1.235 | 0.013 | 0.0017 | 1.97 |

Table 4 and Table 5 show the maximums of acceleration and deceleration of the overtaking vehicle calculated by Eq. 5 and Eq. 19, respectively, using the values in Table 2 and Table 3. The maximum decelerations of the overtaking vehicle on dry surface are supposed to be $60 \%$ of the value calculated by Eq. 19, to provide a safety margin. These accelerations and decelerations were used in computer simulation.

Table 4. Maximum acceleration of overtaking vehicle [ $\mathrm{m} / \mathrm{s}^{2}$ ]

| ascent slope | condition of <br> surface | change in speed of overtaking vehicle |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | $30 \rightarrow 40$ | $45 \rightarrow 60$ | $65 \rightarrow 80$ |
|  | dry | 1.730 | 1.889 | 1.135 |
|  | snowy | 1.342 | 1.342 | 1.135 |
|  | icy | 0.895 | 0.895 | 0.895 |
| $3 \%$ | dry | 1.462 | 1.622 | 0.867 |
|  | snowy | 1.342 | 1.342 | 0.867 |
|  | icy | 0.895 | 0.895 | 0.867 |
| $6 \%$ | dry | 1.195 | 1.354 | 0.600 |
|  | snowy | 1.195 | 1.328 | 0.600 |
|  | icy | 0.895 | 0.895 | 0.600 |

Table 5. Maximum deceleration of overtaking vehicle [ $\mathrm{m} / \mathrm{s}^{2}$ ]

| ascent slope | dry | snowy | icy |
| :---: | :---: | :---: | :---: |
| $0 \%$ | 3.74 | 1.60 | 1.07 |
| $3 \%$ | 3.76 | 1.62 | 1.09 |
| $6 \%$ | 3.77 | 1.64 | 1.10 |

Table 6 shows the supposed vehicle lengths and perception errors.

Table 6. Other settings

| reaction time | vehicle length [m] |  | perception error |  |
| :---: | :---: | :---: | :---: | :---: |
| $: \varepsilon_{1}, \varepsilon_{2}[\mathrm{~s}]$ | compact car | full-size car | $\Delta d$ | $\Delta v$ |
| 0.2 | 4.0 | 10.0 | $0.1 P S D$ | 0.1 V |

## - Results

Table 7 and Table 8 show the $P S D$ when the ascent slope is $0 \%$ for the case of overtaken compact vehicle and overtaken full-size vehicle, respectively. Table 9 and Table 10 show the respective $P S D$ and $D_{R}$ under the supposition that the overtaken vehicle is compact car and full-size car. The upper box and lower box for each surface condition in Table 10 indicate the

Table 7. PSD (both vehicles are compact cars)

|  | ascent slope: 0\% |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | dry ( $\mu=0.7$ ) |  |  | snowy ( $\mu=0.3$ ) |  |  | icy ( $\mu=0.2$ ) |  |  |
| V (km/h) | 80 | 60 | 40 | 80 | 60 | 40 | 80 | 60 | 40 |
| V0 (km/h) | 65 | 45 | 30 | 65 | 45 | 30 | 65 | 45 | 30 |
| $\mathrm{a}(\mathrm{m} / \mathrm{s} 2)$ | 1.135 | 1.889 | 1.73 | 1.135 | 1.342 | 1.342 | 0.895 | 0.895 | 0.895 |
| t1+ $\mathrm{E}_{1}$ ( sec$)$ | 3.9 | 2.4 | 1.8 | 3.9 | 3.3 | 2.3 | 4.9 | 4.9 | 3.3 |
| t2 (sec) | 20.2 | 12.3 | 11.7 | 33.7 | 19.1 | 16.4 | 33.2 | 24.7 | 20.1 |
| t1+t2 $+\varepsilon 1(\mathrm{sec})$ | 24.0 | 14.7 | 13.5 | 37.6 | 22.4 | 18.6 | 38.1 | 29.6 | 23.4 |
| L1* (m) | 46 | 28 | 17 | 74 | 43 | 24 | 74 | 56 | 30 |
| d1 (m) | 78 | 35 | 17 | 78 | 48 | 22 | 97 | 70 | 32 |
| d2 (m) | 448 | 205 | 130 | 749 | 319 | 182 | 738 | 412 | 223 |
| L2* (m) | 46 | 28 | 17 | 74 | 43 | 24 | 74 | 56 | 30 |
| d3 (m) | 60 | 40 | 25 | 60 | 40 | 25 | 60 | 40 | 25 |
| d4 (m) | 534 | 245 | 150 | 835 | 374 | 207 | 846 | 493 | 260 |
| PSD $=\mathrm{d} 1+\mathrm{d} 2+\mathrm{d} 3+\mathrm{d} 4$ (m) | 1119 | 524 | 323 | 1721 | 780 | 435 | 1740 | 1015 | 540 |

Table 8. PSD (overtaken vehicle is full-size car)

|  | ascent slope: 0\% |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | dry ( $\mu=0.7)$ |  |  | snowy ( $\mu=0.3$ ) |  |  | icy ( $\mu=0.2$ ) |  |  |
| V (km/h) | 80 | 60 | 40 | 80 | 60 | 40 | 80 | 60 | 40 |
| V0 ( $\mathrm{km} / \mathrm{h}$ ) | 65 | 45 | 30 | 65 | 45 | 30 | 65 | 45 | 30 |
| $\mathrm{a}(\mathrm{m} / \mathrm{s} 2)$ | 1.135 | 1.889 | 1.73 | 1.135 | 1.342 | 1.342 | 0.895 | 0.895 | 0.895 |
| t1+ $\mathrm{E}_{1}(\mathrm{sec})$ | 3.9 | 2.4 | 1.8 | 3.9 | 3.3 | 2.3 | 4.9 | 4.9 | 3.3 |
| t2 (sec) | 21.6 | 13.7 | 13.9 | 35.1 | 20.6 | 18.5 | 34.6 | 26.2 | 22.2 |
| t1+t2 + ¢ $1(\mathrm{sec})$ | 25.5 | 16.1 | 15.7 | 39.0 | 23.9 | 20.8 | 39.5 | 31.0 | 25.5 |
| L1* (m) | 52 | 34 | 23 | 80 | 49 | 30 | 80 | 62 | 36 |
| d1 (m) | 78 | 35 | 17 | 78 | 48 | 22 | 97 | 70 | 32 |
| d2 (m) | 480 | 229 | 154 | 781 | 343 | 206 | 770 | 436 | 247 |
| L2* (m) | 46 | 26 | 17 | 74 | 43 | 24 | 74 | 56 | 30 |
| d3 (m) | 60 | 40 | 25 | 60 | 40 | 25 | 60 | 40 | 25 |
| d4 (m) | 566 | 269 | 174 | 867 | 398 | 231 | 878 | 517 | 284 |
| PSD $=\mathrm{d} 1+\mathrm{d} 2+\mathrm{d} 3+\mathrm{d} 4$ (m) | 1183 | 572 | 371 | 1785 | 828 | 483 | 1804 | 1063 | 588 |

Table 10. PSD and $D_{R}$ (overtaken vehicle is full-size car)

| ascent slope | surface | changes of | the ove | icle (km |
| :---: | :---: | :---: | :---: | :---: |
| ascent slope | surface | 30-40 | 45-60 | 65-80 |
| 0\% | dry | 371 | 572 | 1183 |
|  |  | 21.0\% | 24.4\% | 29.6\% |
|  | snowy | 483 | 828 | 1785 |
|  |  | 19.3\% | 21.8\% | 27.2\% |
|  | icy | 588 | 1064 | 1805 |
|  |  | 18.5\% | 20.7\% | 24.1\% |
| 3\% | dry | 374 | 578 | 1206 |
|  |  | 21.2\% | 24.6\% | 29.8\% |
|  | snowy | 483 | 828 | 1808 |
|  |  | 19.3\% | 21.8\% | 27.4\% |
|  | icy | 588 | 1064 | 1808 |
|  |  | 18.6\% | 20.9\% | 24.3\% |
| 6\% | dry | 378 | 585 | 1249 |
|  |  | 21.3\% | 24.7\% | 30.1\% |
|  | snowy | 486 | 829 | 1851 |
|  |  | 19.4\% | 21.9\% | 27.7\% |
|  | icy | 588 | 1064 | 1851 |
|  |  | 18.6\% | 20.9\% | 24.7\% |

difference of $P S D$ and $D_{R}$, respectively. Table 11 shows the differences between values in Table 9 and Table 10 (Table 10 - Table 9).

According to Table 11 , the effect of vehicle length on $P S D$ is large. When the speed changes of the overtaking vehicle are $30 \rightarrow 45$ $[\mathrm{km} / \mathrm{h}], 45 \rightarrow 60[\mathrm{~km} / \mathrm{h}]$ and $65 \rightarrow 80[\mathrm{~km} / \mathrm{h}]$, then the differences in $P S D$ are 48 [m], 48 [m] and $64[\mathrm{~m}]$, and these values are not affected by the surface condition nor by the ascent slope. This indicates the difficulty of overtaking full-sized cars. In contrast, the effect of vehicle length on $D_{R}$ is small. That is, $D_{R}$ is little affected by the speed of the overtaking vehicle, the condition of surface and the ascent slope. We know this from Eq. 17, Eq. 18 and Eq. 26. In calculating the $P S D$, the different vehicle lengths affect the space headway (Eq. 17 and Eq. 18); however, this effect is canceled out by the space headway when aborting is finished (Eq. 26). As mentioned above, the vehicle length affects $P S D$, but this effect is a constant determined by the speed of the overtaking vehicle. The vehicle length has little effect on $D_{R}$. For this reason we consider compact cars in the following analysis.

The effect of the speed of overtaking vehicle on PSD is large, according to Table 9. This owes mostly to the safe distance between vehicles. The effect of the speed of overtaking vehicle
on $D_{R}$ is large, too: The greater is the overtaking speed, the larger is $D_{R}$. This does not mean that the faster is the overtaking speed, the easier it is to abort. Instead, the faster is the overtaking speed, the greater is PSD. However, because deceleration is greater than acceleration, the driving distance required for the overtaking vehicle to finish aborting becomes short compared with PSD.

The surface condition affects both $P S D$ and $D_{R}$ according to Table 9 . This indicates that both overtaking and aborting become more difficult on slippery surface, mainly as a result of the decline in acceleration and deceleration of the overtaking vehicle.

The ascent slope affects both $P S D$ and $D_{R}$. However, the differences are not large, according to Table 9. These results are explained by considering that acceleration and deceleration of the overtaking vehicle change according to the ascent slope; however the differences in the acceleration duration and the deceleration duration of overtaking vehicle are not large enough to generate significant differences of $P S D$ and $D_{R}$.

## 6. Conclusions

This study developed a model of overtaking considering slippery road. Acceleration was calculated using both the friction coefficient between tire and road surface and the driving performance curve. The vehicle length, the reaction time of driver and the ascent slope were incorporated into the model. Under the supposition that there is perception error of driver regarding the speed of oncoming vehicle and $P S D$, a model of overtaking aborting also was developed, which defined the safe distance to abort. The ratio of the safe distance to abort to the $P S D$ was defined as the aborting safety ratio.

The following conclusions were obtained.

1) The length of overtaken vehicle, the overtaking vehicle's speed and the friction coefficient between tire and road surface have a large effect on the $P S D$, whereas the ascent slope has no such effect.
2) The overtaking vehicle's speed and the friction coefficient between tire and road surface have a large effect on the safe ratio to abort, whereas the ascent slope and the length of vehicle have no such effect.

## References

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